

# 1 Variation of parameters

$$v_1 = - \int \frac{g(t)y_2}{y_1y_2' - y_1'y_2} dt, \quad v_2 = \int \frac{g(t)y_1}{y_1y_2' - y_1'y_2} dt$$

# 2 Driven harmonic motion

Given  $y'' + 2cy' + \omega_0^2 y = A \cos \omega t$ , the transfer function is given by  $H(\omega) = G(\omega)e^{i(\omega t + \phi(\omega))}$ .

$$G(\omega) = \frac{1}{\sqrt{(\omega_0^2 - \omega^2)^2 + 4c^2\omega^2}}$$

$$-\tan \phi(\omega) = \frac{2c\omega}{\omega_0^2 - \omega^2}$$

# 3 Selected Laplace transforms

Function $u(t)$	Laplace transform $U(s) = \int_0^\infty e^{-st}u(t)dt$
$\alpha f(t) + \beta g(t)$	$\alpha \mathcal{L}[f] + \beta \mathcal{L}[g]$
$e^{ct}f(t)$	$F(s - c), F = \mathcal{L}[f]$
$tf(t)$	$-F'(s), F = \mathcal{L}[f]$
$t^n$	$\frac{n!}{s^{n+1}}$
$\sin(at)$	$\frac{a}{s^2 + a^2}$
$\cos(at)$	$\frac{s}{s^2 + a^2}$
$e^{at}$	$\frac{1}{s - a}$
$e^{at} \sin(bt)$	$\frac{b}{(s - a)^2 + b^2}$
$e^{at} \cos(bt)$	$\frac{s - a}{(s - a)^2 + b^2}$
$t^n e^{at}$	$\frac{n!}{(s - a)^{n+1}}$
$y'(t)$	$s\mathcal{L}[y] - y(0)$
$y''(t)$	$s^2\mathcal{L}[y] - sy(0) - y'(0)$
$H(t - c)$	$\frac{e^{-cs}}{s}$
$H(t - c)f(t - c)$	$e^{-cs}\mathcal{L}[f]$
$f(t)$	$\frac{\mathcal{L}[f_T]}{1 - e^{-Ts}}$ (if $f$ has period $T$ )
$\delta(t - c)$	$e^{-cs}$
$f * g$	$\mathcal{L}[f]\mathcal{L}[g]$

Here  $f * g$  is defined as  $\int_0^t f(u)g(t - u)du$ .